

# Chaotic Interaction of Bubbles under Forced Vibration in Microgravity

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## Motivation

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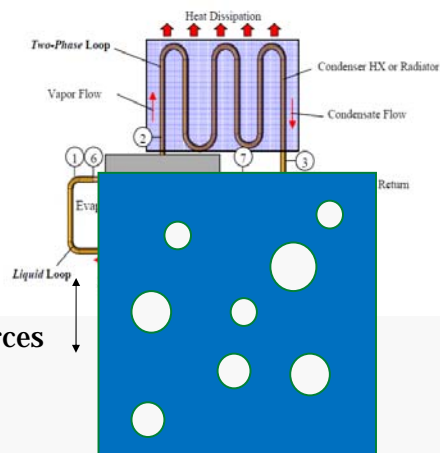
### □ Phase separation in microgravity

#### □ Applications:

- Liquid recycling
- Water purification
- Thermal management

#### □ Methods:

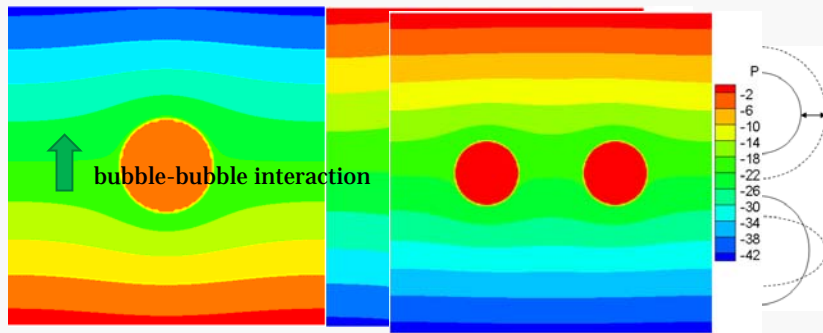
- Centrifugal force
- Thermo-capillary force
- Electric and magnetic forces
- Vibration-induced forces



# Oscillatory Body Force

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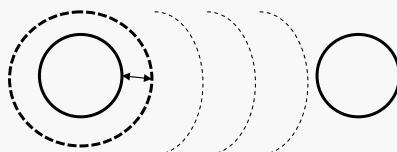
oscillatory buoyancy force



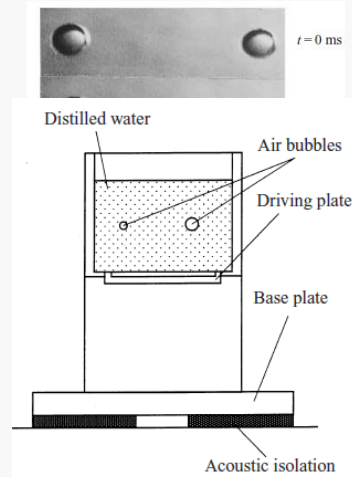
# Bubble-Bubble Interaction

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bubble-bubble interaction in acoustic fields



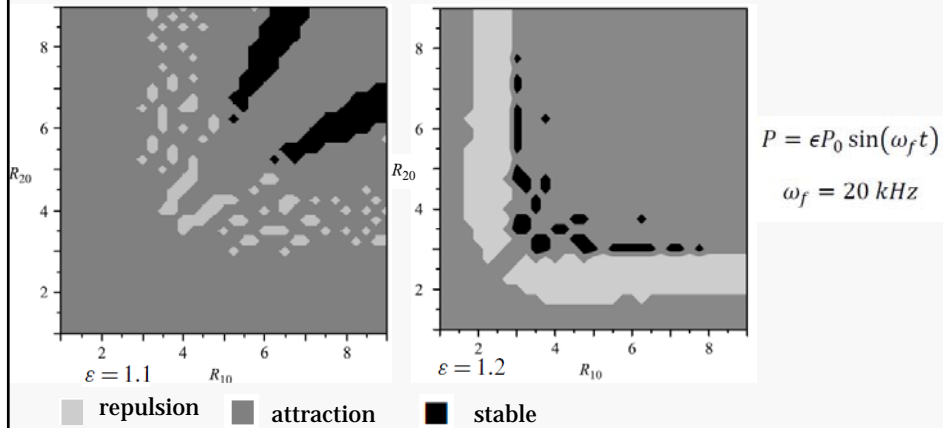
pressure wave ( $\nabla p$ ) from volume oscillation



from Barbat and Ashgriz-JFM (389)-1999

# Interaction Map

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# Translational Motion

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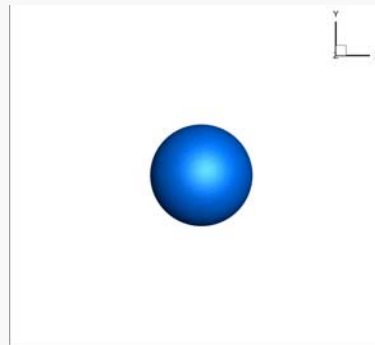
$F_b = \text{buoyancy force}$

$F_d = \text{drag force}$

$F_a = \text{added mass force}$

$$\sum F = F_b + F_d + F_a = m_b a$$

$$F_a = \begin{cases} c(\alpha, \beta) \frac{4}{3} \pi a^2 b \rho \frac{dU}{dt} & \text{Shape Change} \\ \frac{1}{2} \rho \frac{d}{dt}(UV) & \text{Volume Change} \end{cases}$$



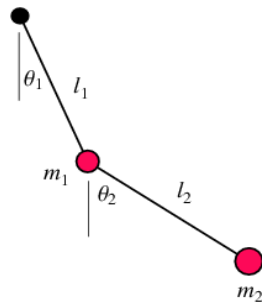
$R = 3 \text{ mm}$   
 $f = 100 \text{ Hz}$   
 $Ac = 0.2 \text{ mm}$

Oscillatory translational motion and shape/volume change are coupled

# Coupled Nonlinear Systems

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- Double Pendulum problem
  - Two coupled nonlinear systems
  - Chaotic motion, sensitive to initial conditions



## Objective

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- Determine conditions under which bubble behavior becomes chaotic.
  - Study chaotic/regular behavior of bubbles under forced vibration
    - Identify regions where the bubble oscillation turns chaotic as a function of vibration amplitude, frequency, and bubble radius
    - Investigate if the chaotic motion can enhance the separation process or lead to the formation of smaller bubbles.

# Objective

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- Study bubble-bubble interaction under forced oscillation
  - Identify attraction, repulsion and oscillation regions based on vibration amplitude, frequency, and bubbles radii

# Numerical Model

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- Governing equations to be solved

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \vec{V}) = 0$$

$$\frac{\partial \vec{V}}{\partial t} + \vec{V} \cdot \nabla \vec{V} = -\frac{1}{\rho} \nabla p + \frac{1}{\rho} \nabla \cdot T + \vec{F}_b \quad \vec{F}_b = A_c \omega^2 \sin(\omega t)$$

Two-dimensional-  
incompressible

Three dimensional-  
incompressible/ compressible



Code developed by Bussmann et al.

TransAT®

# Numerical Model

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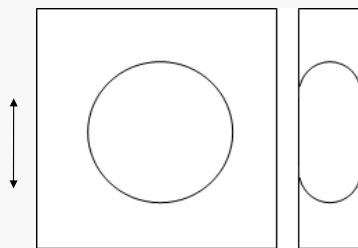
$$\begin{cases} f = 0 & \text{gas} \\ 0 < f < 1 & \text{Interface} \\ f = 1 & \text{liquid} \end{cases}$$

$$\frac{\partial f}{\partial t} + (\vec{v} \cdot \nabla) f = 0$$

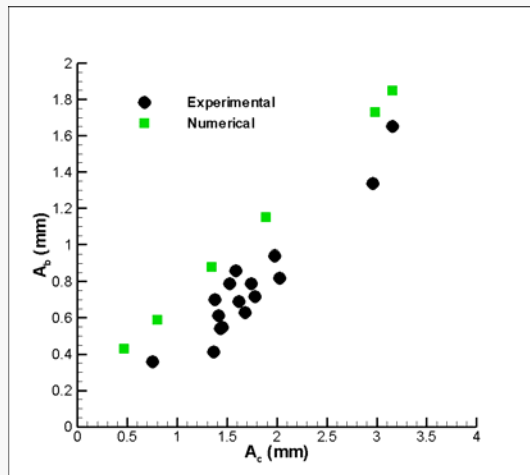
1	1	1	.68	0
1	1	1	.42	0
1	1	.92	.09	0
1	.85	.35	0	0
.31	.09	0	0	0
0	0	0	0	0

# Comparison to Experiments

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$$\begin{aligned} R &= 2.6 \text{ cm} \\ \rho_l &= 1000 \text{ kg/m}^3 \\ \rho_g &= 1 \text{ kg/m}^3 \\ \sigma &= 0.022 \text{ N/m} \\ \omega &= 2\pi f, f = 0.6 \text{ Hz} \end{aligned}$$

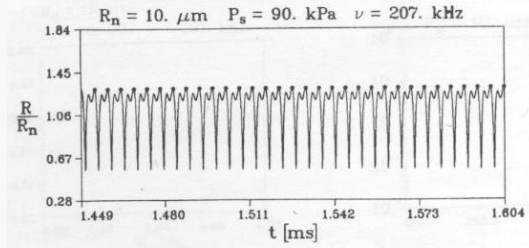


ISCAP project conducted during STS-85 mission in August 1997

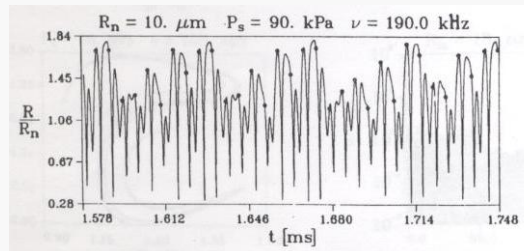
# Regular VS Chaotic

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Regular



Chaotic



Lauterborn and Parlitz,  
J. Acoust. Soc. Am. (84)- 1988

# Shape Decomposition

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$$r = R + \sum_{n=0}^{\infty} C_n(t) P_n(\cos(\theta)) = R + C_1(t)P_1(\cos \theta) + C_2(t)P_2(\cos \theta) + C_3(t)P_3(\cos \theta) + \dots$$

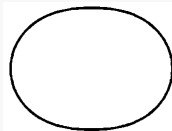
Arbitrary shape



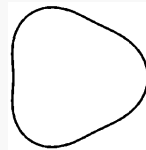
=



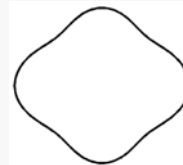
+



$$P_2 = \frac{1}{2}(3\cos^2 t - 1)$$



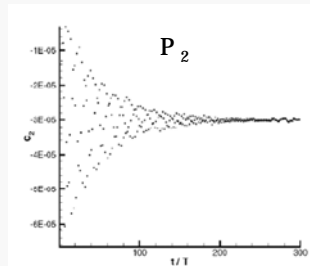
$$P_3 = \frac{1}{2}(5\cos^3 t - 3)$$



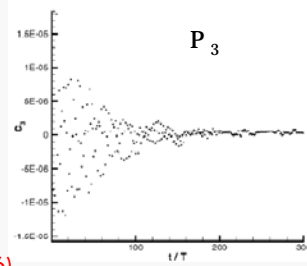
$$P_4 = \frac{1}{8}(35\cos^4 t - 30\cos^2 t + 3)$$

# Regular Oscillation

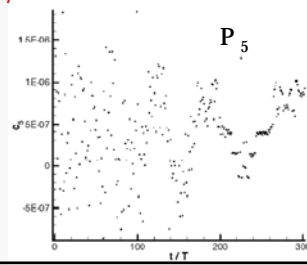
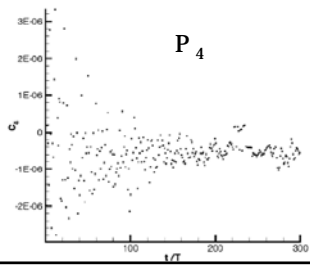
15



$\sigma$  ( $1e-6$ )

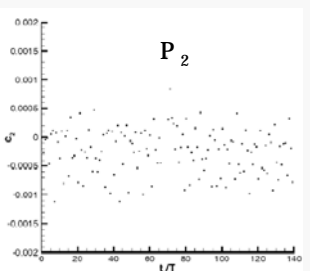


$R = 2 \text{ mm}$   
 $f = 100 \text{ Hz}$   
 $A_c = 0.1 \text{ mm}$

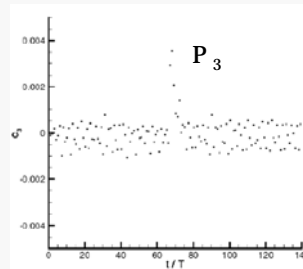


# Chaotic Oscillation

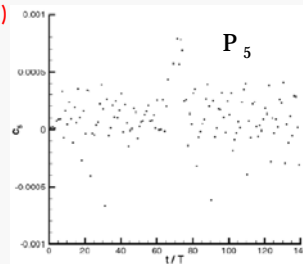
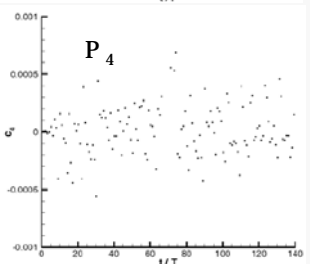
16



$\sigma$  ( $1e-4$ )



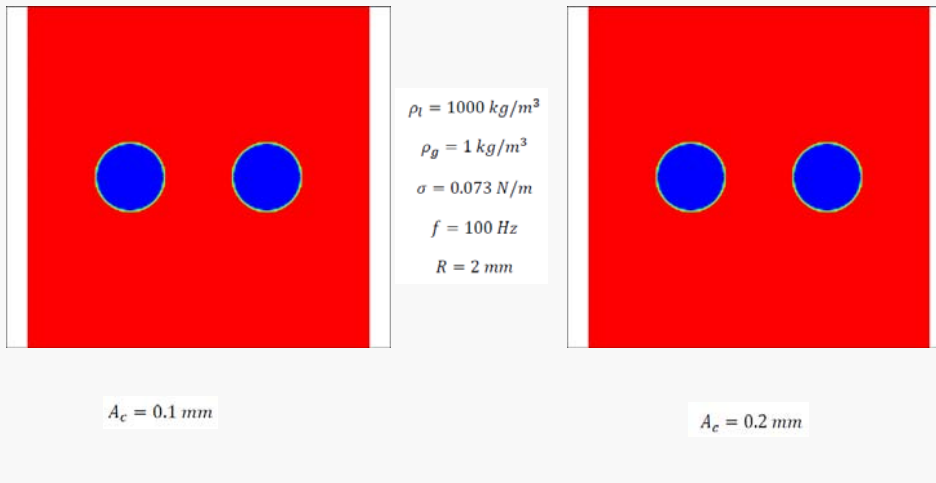
$R = 2 \text{ mm}$   
 $f = 100 \text{ Hz}$   
 $A_c = 0.2 \text{ mm}$





# Bubble-Bubble Interaction

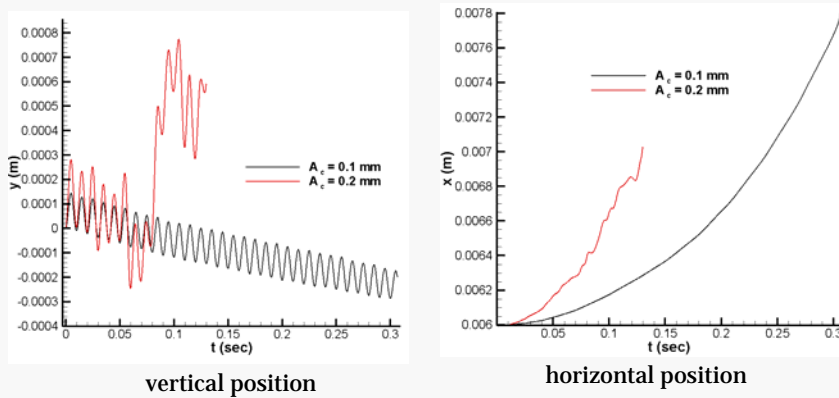
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# Vibration Amplitude Effect

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Vibration Amplitude Effect  
 $f = 100 \text{ Hz}$ ,  $\sigma = 0.073 \text{ N/m}$ ,  $\rho_l / \rho_g = 1000/1$



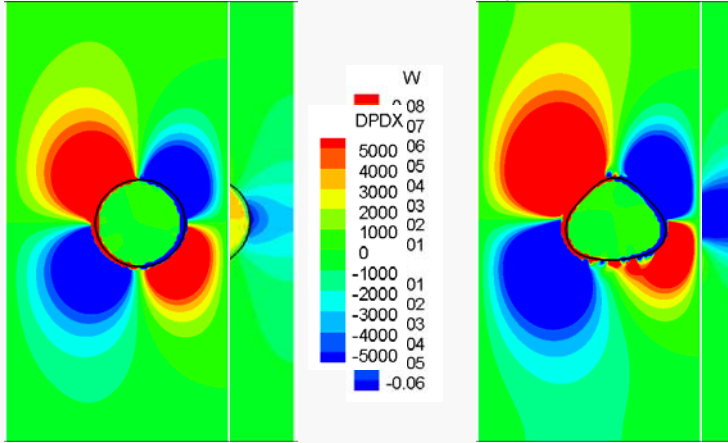
Left bubble motion

# Vibration Amplitude Effect

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## Vibration Amplitude Effect- left bubble

$f = 100 \text{ Hz}$ ,  $\sigma = 0.073 \text{ N/m}$ ,  $\rho_l / \rho_g = 1000/1$



$A_v = 0.1 \text{ mm}$   
 $A_c = 0.1 \text{ mm}$

Vertical velocity at  $t = 5.25 \text{ T}$  (m/s)  
Horizontal pressure gradient at  $t = 5 \text{ T}$  (Pa/m)

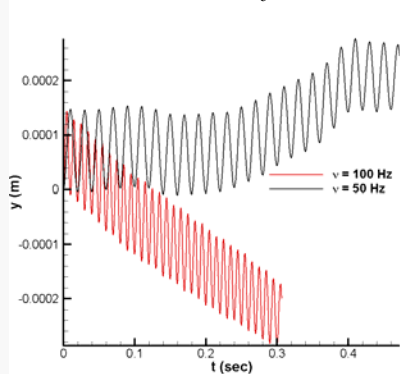
$A_v = 0.2 \text{ mm}$   
 $A_c = 0.2 \text{ mm}$

# Vibration Frequency Effect

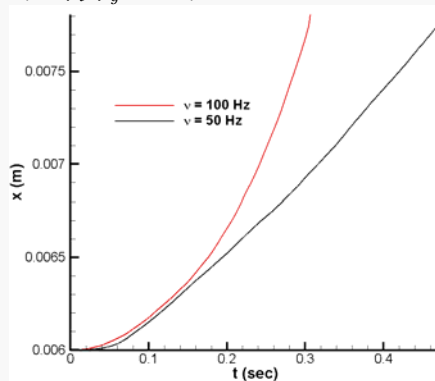
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## Vibration frequency Effect

$A_c = 0.1 \text{ mm}$ ,  $\sigma = 0.073 \text{ N/m}$ ,  $\rho_l / \rho_g = 1000/1$



vertical position



horizontal position

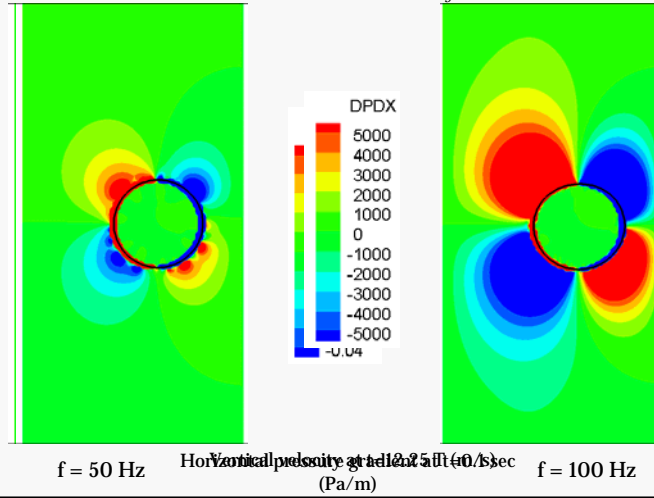
Left bubble motion

# Vibration Frequency Effect

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Vibration frequency Effect- left bubble

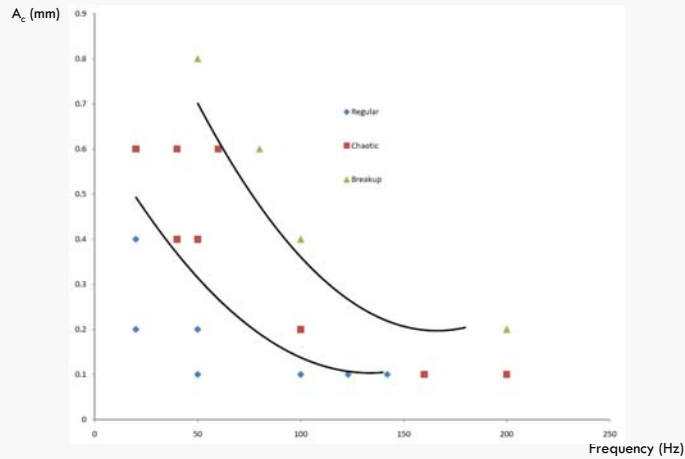
$$A_c = 0.1 \text{ mm}, \sigma = 0.073 \text{ N/m}, \rho_l / \rho_g = 1000/1$$



# Bubble Behavior

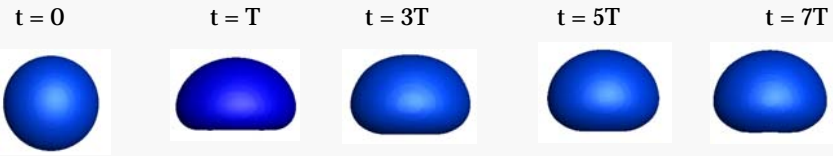
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Effect of vibration amplitude and frequency on the shape of the bubbles before collision for  $R = 2 \text{ mm}$

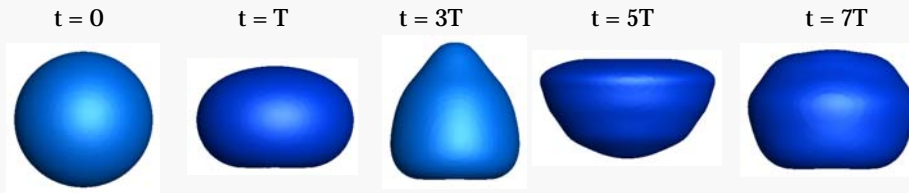


# 3D Results

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$R = 2 \text{ mm}, f = 100 \text{ Hz}, A_c = 0.2 \text{ mm}$

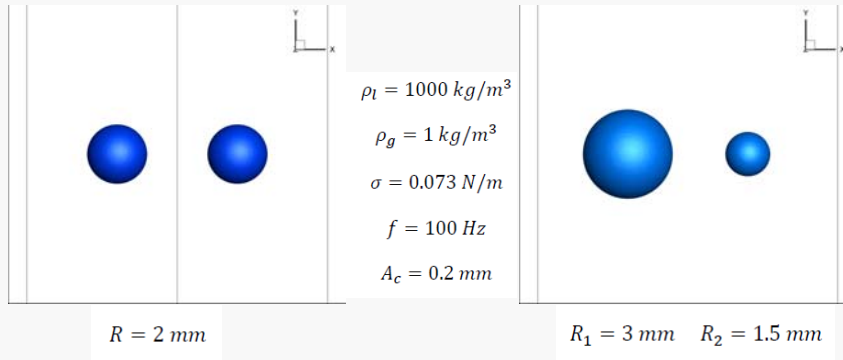


$R = 3 \text{ mm}, f = 100 \text{ Hz}, A_c = 0.2 \text{ mm}$

# 3D Bubble-Bubble Interaction

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## □ Bubble-bubble interaction



## Conclusions

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- Oscillatory translational motion and shape deformation of bubbles are strongly coupled.
- This coupled system can become chaotic under certain conditions.
- The chaotic behavior is characterized based on the behavior of the Legendre polynomial coefficients which represent the shape of the bubble.
- The onset of chaotic behavior depends on the bubble size, vibration amplitude and frequency.

## Conclusions

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- In smaller bubble sizes, amplitudes, and frequencies surface tension force stabilizes the motion and prevents chaos.
- As a results of the flow fields developed around each bubble, bubble-bubble interaction occurs. In this study, outcome of the interaction was attraction.
- Higher vibration amplitude and frequency enhances the bubble interaction and attraction.
- Possibility of bubble breakup to smaller bubbles also increases in higher amplitudes and frequencies.

**Thank You**